

ECE 3056 Project 2 Report

Ruoyang Xu

Last Edited Date: October 19, 2018

Contents

1	Cache Data structure	2
1.1	Cache Directory Structure	2
1.2	LRU Stack	2
2	Cache Configuration Plots	2
2.1	Miss rate vs Line Size	2
2.2	Miss Rates under Best Configuration	2
2.3	Writeback Traffic	3
2.4	Total Memory Access Volume	3
3	Plot for Miss rates and Data Calculation of Best Configuration	4

1 Cache Data structure

1.1 Cache Directory Structure

The data structure implemented for cache directory is a 2D dynamically allocated struct array. The struct is a three integer struct that contains the tag, valid and dirty information for one single cache line. The number of rows in the array is defined by the number of cache lines in every associative set. The number of columns is defined by the number of associative set. Valid and Dirty value are initialized to be 0 and tag value initialized to -1.

1.2 LRU Stack

The implementation of LRU stack is built on top of another 2D array. The number of row and column of the 2D array is also defined by the number of cache lines in every set and the set number respectively. Every row of LRU is a stack, with value in index 0 to be the least recently used memory index in cache and value stored in right most location to be the most recently used.

When updating the LRU (no write back) with index i in cache. The program would traverse the LRU stack at the corresponding line, find index i , shift the array and place index i in the rightmost spot. When a write back action is required, the LRU stack would return value stored at index 0 to its caller, stating that the memory located at this value location is the least recently used. The LRU stack would then shift leftwards by one position and place the returned value at most recently used spot.

2 Cache Configuration Plots

2.1 Miss rate vs Line Size

Line size from 32 byte to 512 byte, fixed associativity of 4. See Figure 1, 2, 3 and 4, at the end of docuemnt.

2.2 Miss Rates under Best Configuration

The assignment asks to compute the miss rate using the best overall configuration that minimizes the **sum of the overall miss rate across all traces**. Overall miss rate is calculated by $1 - \frac{\sum Hits_{Traces}}{\sum Access_{traces}}$. The resulting configuration is Way count = 8, Block Size = 512. The computation of miss rates can be seen in Table 1. trace.stream1M and trace.random64k has N/A values for Write miss since it only contains read instructions and no write.

Trace Name	Overall Miss	Read Miss	Write Miss
trace.stream1M	0.7812%	0.7812%	N/A
trace.random64k	50.0915%	50.0915%	N/A
trace.merge	0.1976%	0.2102%	0.1247%
trace.bubble	0.1845%	0.1926%	0.1145%

Table 1: Overall, write & read miss rate for all traces with minimum overall sum miss rate.

2.3 Writeback Traffic

The configuration is the same as 2.2. trace.stream1M and trace.random64k have 0 writeback traffic since there's no write instruction that invoke these actions.

Trace Name	Writeback Traffic
trace.stream1M	0
trace.random64k	0
trace.merge	1744896
trace.bubble	1166336

Table 2: Write back traffic for all traces in bytes.

2.4 Total Memory Access Volume

Minimum sum memory access is Way count = 8, Block size = 32 byte.

Trace Name	Memory Access	Memory Referenced	Amount saved
trace.stream1M	1048576	8388608	7340032
trace.random64k	4203680	8388608	4184928
trace.merge	1296320	245709760	244413440
trace.bubble	718208	202314976	201596768

Table 3: Memory accessed and referenced for all traces in bytes

Compared to total referenced memory, using cache greatly saved the number of memory access count and reduces the time for instructions. The lower the miss rate, the higher the amount of memory saved from accessing the memory by having the cache.

3 Plot for Miss rates and Data Calculation of Best Configuration

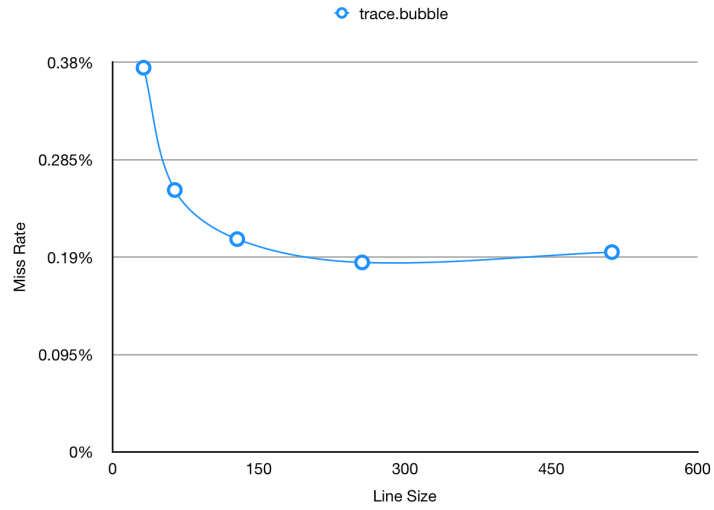


Figure 1: Miss rate vs Line size for trace.bubble test case

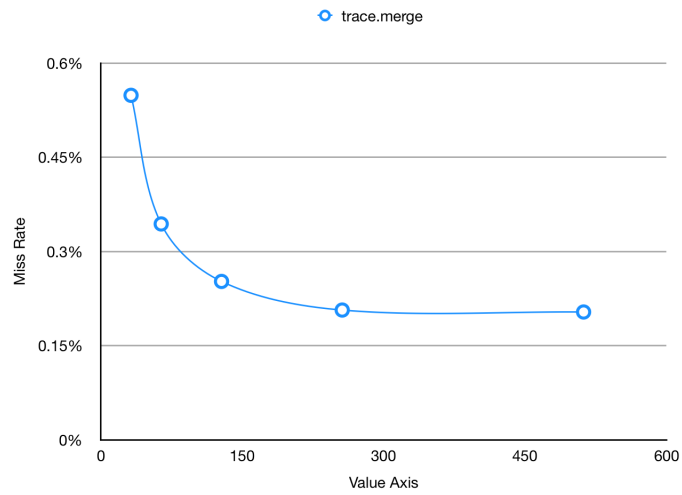


Figure 2: Miss rate vs Line size for trace.merge test case

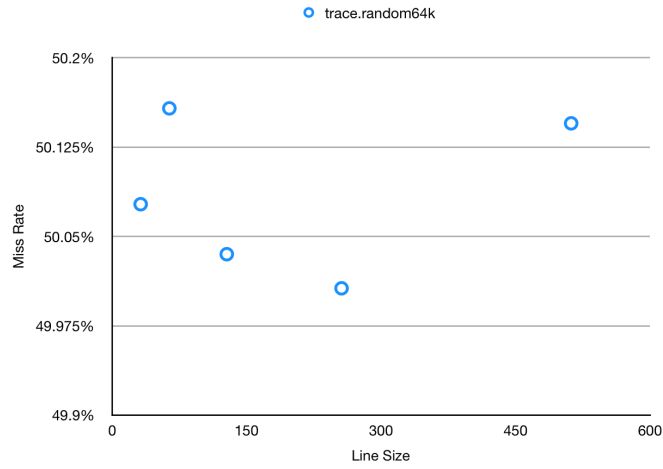


Figure 3: Miss rate vs Line size for trace.random64k test case

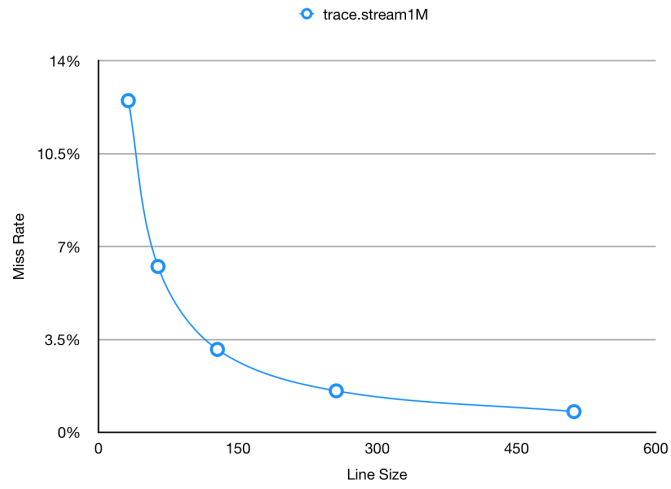
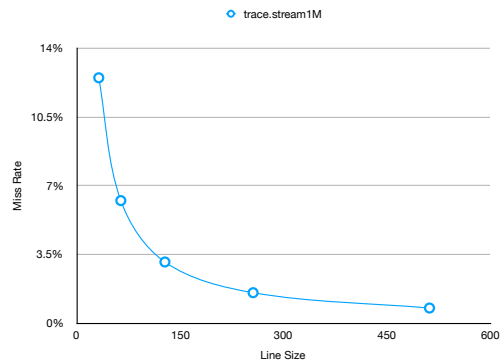
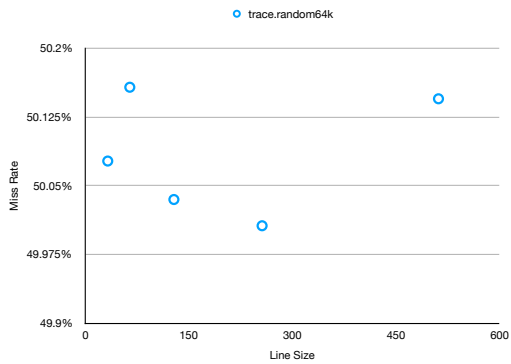
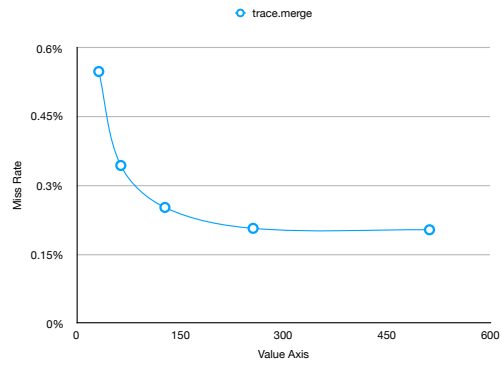
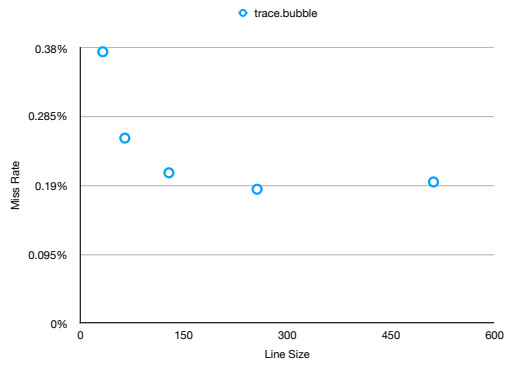


Figure 4: Miss rate vs Line size for trace.stream1M test case

Table for Question 1

	Block Size	Cache Size	Ways Count	Access Count	Read Access	Write Access	Total Hits	Read Hits	Write Hits	Writeback traffic	Total Access Volume	Miss rate, in percentage
trace.bubble	32	64000	4	6322343	5666010	656333	6298650	5649037	649613	245152	758176	0.374750310130278%
trace.bubble	64	64000	4	6322343	5666010	656333	6306191	5653394	652797	303936	1033728	0.255474908590059%
trace.bubble	128	64000	4	6322343	5666010	656333	6309218	5654842	654376	423424	1680000	0.207597088610978%
trace.bubble	256	64000	4	6322343	5666010	656333	6310655	5655486	655169	653312	2992128	0.184868173080766%
trace.bubble	512	64000	4	6322343	5666010	656333	6310020	5654467	655553	1213440	6309376	0.194911917939278%
trace.merge	32	64000	4	7678430	6544752	1133678	7636301	6516507	1119794	554368	1348128	0.548666849863844%
trace.merge	64	64000	4	7678430	6544752	1133678	7652035	6525615	1126420	630080	1689280	0.343755168699855%
trace.merge	128	64000	4	7678430	6544752	1133678	7659065	6529331	1129734	779264	2478720	0.252199994009195%
trace.merge	256	64000	4	7678430	6544752	1133678	7662567	6531124	1131443	1063424	4060928	0.206591712107818%
trace.merge	512	64000	4	7678430	6544752	1133678	7662804	6530502	1132302	1773568	8000512	0.203505143629623%
trace.random64k	32	64000	4	262144	262144	0	130670	130670	0	0	4200768	50.0770568847656%
trace.random64k	64	64000	4	262144	262144	0	130659	130659	0	0	8415040	50.1575469970703%
trace.random64k	128	64000	4	262144	262144	0	130980	130980	0	0	1678992	50.0350952148438%
trace.random64k	256	64000	4	262144	262144	0	131055	131055	0	0	33558784	50.0064849853516%
trace.random64k	512	64000	4	262144	262144	0	130692	130692	0	0	67303424	50.1449584960938%
trace.stream1M	32	64000	4	262144	262144	0	229376	229376	0	0	1048576	12.5%
trace.stream1M	64	64000	4	262144	262144	0	245760	245760	0	0	1048576	6.25%
trace.stream1M	128	64000	4	262144	262144	0	253952	253952	0	0	1048576	3.125%
trace.stream1M	256	64000	4	262144	262144	0	258048	258048	0	0	1048576	1.5625%
trace.stream1M	512	64000	4	262144	262144	0	260096	260096	0	0	1048576	0.78125%



Best Configuration Marked in Green

Table for Question 2 to 4

Block Size	Cache Size	Ways Count	Access Count	Memory Referenced	Read Access	Write Access	Total Hits	Read Hits	Write Hits	Writeback traffic	Total Access Volume	Overall Miss	Read Miss	Write Miss	Overall miss rate =	Total Memory Access	Total Memory referenced
trace.stream1M	32	64000	2	282144	898608	282144	0	229376	229376	0	0	12.5%	12.5%	12.5%	1.61929096201386%	7526496	464801952
trace.random64k	32	64000	2	282144	8386608	282144	0	130951	130951	0	0	50.0461578369141%	50.0461578369141%	50.0461578369141%	1.61929096201386%	7526496	464801952
trace.merge	32	64000	2	7678430	245709760	6544752	1133678	7633371	6513841	1119530	576448	0.58682569223352%	0.472302082645759%	1.24797341043933%	1.61929096201386%	7526496	464801952
trace.bubble	32	64000	2	6322343	202314976	5666010	656333	6296160	5646620	649540	256512	0.414134443512482%	0.342216127398287%	1.03499290756369%	1.5825338014071%	7355648	464801952
trace.stream1M	32	64000	4	282144	8986608	282144	0	229376	229376	0	0	12.5%	12.5%	12.5%	1.5825338014071%	7355648	464801952
trace.random64k	32	64000	4	282144	8386608	282144	0	130870	130870	0	0	50.0770568847656%	50.0770568847656%	50.0770568847656%	1.5825338014071%	7355648	464801952
trace.merge	32	64000	4	7678430	245709760	6544752	1133678	7636301	6516507	1119794	543368	0.548666849863844%	0.431567154874624%	1.22468637479073%	1.5825338014071%	7355648	464801952
trace.bubble	32	64000	4	6322343	202314976	5666010	656333	6296850	5649037	649613	245152	0.37475031030278%	0.299556242925801%	1.02387050475902%	1.5825338014071%	7355648	464801952
trace.stream1M	32	64000	8	282144	8386608	282144	0	229376	229376	0	0	12.5%	12.5%	12.5%	1.56341512094166%	7266784	464801952
trace.random64k	32	64000	8	282144	8386608	282144	0	130779	130779	0	0	50.1117706298828%	50.1117706298828%	50.1117706298828%	1.56341512094166%	7266784	464801952
trace.merge	32	64000	8	7678430	245709760	6544752	1133678	7637920	6518162	1119758	543456	0.527581810344047%	0.406279718467562%	1.22786187965189%	1.56341512094166%	7266784	464801952
trace.bubble	32	64000	8	6322343	202314976	5666010	656333	6299899	5650202	649697	241504	0.35499497575503%	0.278997036715434%	1.0110712344953%	1.56341512094166%	7266784	464801952
trace.stream1M	64	64000	2	282144	16777216	282144	0	245760	245760	0	0	6.25%	6.25%	6.25%	1.34721637313606%	12523776	929603904
trace.random64k	64	64000	2	282144	16777216	282144	0	130649	130649	0	0	50.1613616943359%	50.1613616943359%	50.1613616943359%	1.34721637313606%	12523776	929603904
trace.merge	64	64000	2	7678430	491419520	6544752	1133678	7649009	6522862	1126147	674560	0.383164286653468%	0.334466454955051%	0.664297975262818%	1.34721637313606%	12523776	929603904
trace.bubble	64	64000	2	6322343	404629952	5666010	656333	6303959	5651251	652708	323712	0.290778276344705%	0.260483126574085%	0.552311098177294%	1.34721637313606%	12523776	929603904
trace.stream1M	64	64000	4	282144	16777216	282144	0	245760	245760	0	0	6.25%	6.25%	6.25%	1.31094802286889%	12186624	929603904
trace.random64k	64	64000	4	282144	16777216	282144	0	130659	130659	0	0	50.1575469970703%	50.1575469970703%	50.1575469970703%	1.31094802286889%	12186624	929603904
trace.merge	64	64000	4	7678430	491419520	6544752	1133678	7652035	6525615	1126420	630080	0.343755168698855%	0.29240221783805%	0.640217063398951%	1.31094802286889%	12186624	929603904
trace.bubble	64	64000	4	6322343	404629952	5666010	656333	6306191	5653394	652797	303936	0.255474908590059%	0.222661096609439%	0.538750908456531%	1.31094802286889%	12186624	929603904
trace.stream1M	128	64000	2	282144	16777216	282144	0	245760	245760	0	0	6.25%	6.25%	6.25%	1.29212538246828%	12011648	929603904
trace.random64k	128	64000	2	282144	16777216	282144	0	130813	130613	0	0	50.1750946044922%	50.1750946044922%	50.1750946044922%	1.29212538246828%	12011648	929603904
trace.merge	128	64000	2	7678430	491419520	6544752	1133678	7653622	6527182	1126440	611776	0.323086881042089%	0.268459370194618%	0.638452894031638%	1.29212538246828%	12011648	929603904
trace.bubble	128	64000	2	6322343	404629952	5666010	656333	6307384	5654526	652858	291584	0.236605321792882%	0.202682310832492%	0.529456845838927%	1.29212538246828%	12011648	929603904
trace.stream1M	128	64000	2	282144	33554432	282144	0	253952	253952	0	0	3.125%	3.125%	3.125%	1.18310002278131%	21996288	1859207808
trace.random64k	128	64000	2	282144	33554432	282144	0	130955	130955	0	0	50.0446319580078%	50.0446319580078%	50.0446319580078%	1.18310002278131%	21996288	1859207808
trace.merge	128	64000	2	7678430	982839040	6544752	1133678	7659065	6529331	1129734	779264	0.252199994009195%	0.235623901409865%	0.3478941992347%	1.18310002278131%	21996288	1859207808
trace.bubble	128	64000	2	6322343	809259904	5666010	656333	6309218	5654842	423424	1680000	0.20759708610978%	0.191705193954827%	0.298171812174608%	1.18310002278131%	21996288	1859207808
trace.stream1M	128	64000	8	282144	33554432	282144	0	253952	253952	0	0	3.125%	3.125%	3.125%	1.1595476259862%	21558400	1859207808
trace.random64k	128	64000	8	282144	33554432	282144	0	130825	130825	0	0	50.0942230224609%	50.0942230224609%	50.0942230224609%	1.1595476259862%	21558400	1859207808
trace.merge	128	64000	8	7678430	982839040	6544752	1133678	7660994	6531214	1129780	745856	0.227077670825937%	0.206852757751552%	0.343838660968874%	1.1595476259862%	21558400	1859207808
trace.bubble	128	64000	8	6322343	809259904	5666010	656333	6310885	5656438	654427	1469184	0.181546619662998%	0.168937223801833%	0.290401386379567%	1.1595476259862%	21558400	1859207808
trace.stream1M	256	64000	2	282144	67108864	282144	0	258048	258048	0	0	1.5625%	1.5625%	1.5625%	1.16714139789155%	43399168	3718415616
trace.random64k	256	64000	2	282144	67108864	282144	0	130866	130866	0	0	50.0785827636719%	50.0785827636719%	50.0785827636719%	1.16714139789155%	43399168	3718415616
trace.merge	256	64000	2	7678430	1965675080	6544752	1133678	7658019	6527411	1130608	1402880	0.265822570499441%	0.2649603853525614%	0.270799997882998%	1.16714139789155%	43399168	3718415616
trace.bubble	256	64000	2	6322343	1618519808	5666010	656333	6308600	5653559	655041	737536	0.217371945811862%	0.219748994442393%	0.196851293474488%	1.16714139789155%	43399168	3718415616
trace.stream1M	256	64000	4	282144	67108864	282144	0	258048	258048	0	0	1.5625%	1.5625%	1.5625%	1.132083695484%	41680416	3718415616
trace.random64k	256	64000	4	282144	67108864	282144	0	131055	131055	0	0	50.0064849853516%	50.0064849853516%	50.0064849853516%	1.132083695484%	41680416	3718415616
trace.merge	256	64000	4	7678430	1965675080	6544752	1133678	7662567	6531124	1131443	1063424	0.206591712107818%	0.208227905350733%	0.197145926797559%	1.132083695484%	41680416	3718415616
trace.bubble	256	64000	4	6322343	1618519808	5666010	656333	6310655	5655486	655169	653312	0.184868173080766%	0.185739170950983%	0.177946998145754%	1.132083695484%	41680416	3718415616
trace.stream1M	256	64000	8	282144	67108864	282144	0	258048	258048	0	0	1.5625%	1.5625%	1.5625%	1.10378193936672%	41043200	3718415616
trace.random64k	256	64000	8	282144	67108864	282144	0	131107	131107	0	0	49.986848595703%	49.986848595703%	49.986848595703%	1.10378193936672%	41043200	3718415616
trace.merge	256	64000	8	7678430	1965675080	6544752	1133678	7663984	6532440	1131444	1021440	0.189439788285959%	0.188120191567231%	0.197057718329186%	1.10378193936672%	41043200	3718415616
trace.bubble	256	64000	8	6322343	1618519808	5666010	656333	6311897	5656494	655203	610816	0.168386941360188%	0.167948874075408%	0.17218870094906%	1.10378193936672%	41043200	3718415616
trace.stream1M	512	64000	2	282144	13421728	282144	0	260096	260096	0	0	0.78125%	0.78125%	0.78125%	1.16870421404771%	86914560	7436831232
trace.random64k	512	64000	2	282144	13421728	282144	0	130834	130834	0	0	50.0907897949219%	50.0907897949219%	50.0907897949219%	1.16870421404771%	86914560	7436831232
trace.merge	512	64000	2	7678430	3931356160	6544752	1133678	7656393	6525859	1130534	11282944	0.286998774489056%	0.286674039902503%	0.277327424542062%	1.16870421404771%	86914560	7436831232
trace.bubble	512	64000	2	6322343	3237039616	5666010	656333	6307983	5652605	655378	1452032	0.227130986091706%	0.236586239699543%	0.145505406554292%	1.16870421404771%	86914560	7436831232
trace.stream1M	512	64000	4	282144	13421728	282144	0	260096	260096	0	0	0.78125%	0.78125%	0.78125%	1.11152028896815%	82061888	7436831232
trace.random64k	512	64000	4	282144	13421728	282144	0	130692	130692	0	0	50.1449584960938%	50.1449584960938%	50.1449584960938%	1.11152028896815%	82061888	7436831232
trace.merge	512	64000	4	7678430	3931356160	6544752	1133678	7662804	6305052	1132302	1773568	0.203505143629623%	0.21773170320206%	0.121374852471334%	1.11152028896815%	82061888	7436831232
trace.bubble	512	64000	4	6322343	3237039616	5666010	656333	6310220	5654467	655553	1213440	0.194911917939278%	0.20372560797104%	0.118842112159534%	1.11152028896815%	82061888	7436831232
trace.stream1M	512	64000	8	282144	13421728	282144	0	260096	260096	0	0	0.78125%	0.78125%	0.78125%	1.1029626656986%	82025472	7436831232
trace.random64k	512	64000	8	282144	13421728	282144	0	130832	1308								